Modified Atwood's Machines Lesson Notes

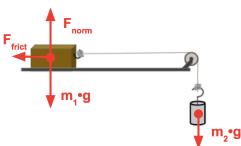
Learning Outcomes

 How do you use a free-body diagram and Newton's second law to analyze and solve a modified Atwood's Machine problem?

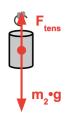
The Bsic Approach

A modified Atwood's Machine problem can be analyzed in two steps.

A System Analysis
 Relate the acceleration to the mass values.

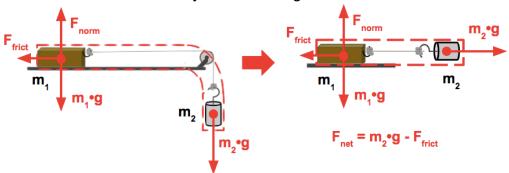


An Individual
 Object Analysis
 Relate the tension
 in the string to the
 acceleration and the
 mass values.



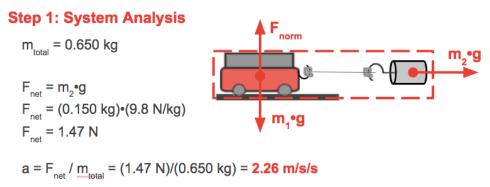
Straightening Out the System

A convenient strategy involves picturing the gravity force on the hanging mass to be a horizontal force that accelerates the system to the right.



Example 1:

A 0.150-kg hanging mass (m₁) is attached by a string to a 0.500-kg cart (m₂) at rest on a friction-free table. Calculate the acceleration of the cart and the tension in the string.

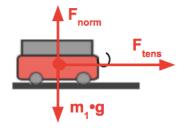


Step 2: Individual Object Analysis

Consider
$$\mathbf{m}_1$$
: $\mathbf{m}_1 = 0.500 \text{ kg}$

$$F_{net} = m_1 \cdot a$$

 $F_{net} = (0.500 \text{ kg}) \cdot (2.26 \text{ m/s/s})$
 $F_{net} = 1.13 \text{ N}$



The vertical forces balance. The tension force is the one unbalanced force that causes the acceleration. It equals F_{net}.

Example 2:

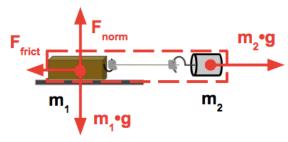
A 0.250-kg hanging mass (m_2) is attached by a string to a 0.500-kg block (m_1) at rest on a table. The coefficient of friction (μ) is 0.215. Calculate the acceleration of the cart and the tension in the string.

Step 1: System Analysis

$$m_{total} = 0.750 \text{ kg}$$

$$m_2 \cdot g = (0.250 \text{ kg}) \cdot (9.8 \text{ N/kg}) = 2.45 \text{ N}$$

$$\begin{split} F_{frict} &= \mu \bullet F_{norm} = \mu \bullet m_{1} \bullet g \\ F_{frict} &= (0.215) \bullet (0.500 \text{ kg}) \bullet (9.8 \text{ N/kg}) \\ F_{frict} &= 1.05 \text{ N} \quad (1.0535 \text{ N}) \end{split}$$



$$F_{net} = m_2 \cdot g - F_{frict} = 2.45 \text{ N} - 1.05 \text{ N} = 1.40 \text{ N}$$

 $a = F_{net} / m = (1.40 \text{ N})/(0.750 \text{ kg}) = 1.86 \text{ m/s/s}$

Step 2: Individual Object Analysis

Consider
$$m_2$$
: $m_2 = 0.250 \text{ kg}$

$$m_{2} \cdot g = (0.250 \text{ kg}) \cdot (9.8 \text{ N/kg}) = 2.45 \text{ N}$$

$$F_{net} = m_2 \cdot a = (0.250 \text{ kg}) \cdot (1.86 \text{ m/s/s})$$

 $F_{net} = 0.466 \text{ N} \quad (0.4655 \text{ N})$

